

Series 11 - The Schottky junctionExercise

The aim of this series is to consider the case of metal-semiconductor contacts. As we will see, such a contact can exhibit a rectifying behavior originating from the potential barrier which is formed at the metal-semiconductor interface due to the presence of a space charge region on the semiconductor side. The model which results from this concept is the so-called Schottky barrier or Schottky junction. Metal-semiconductor contacts can also exhibit a non-rectifying behavior, i.e. the contact will have a negligible resistance whatever the applied potential. The latter case corresponds to the Ohmic contact and it is the type of contact which is required to connect a semiconductor device or an integrated circuit to other devices in an electronic system.

As quoted in the problem working at the surface of a semiconductor the crystal periodicity is broken. The dangling bonds which result from this configuration are not fully hybridized. Qualitatively, we can understand that the wave function associated with such a dangling bond will not possess the delocalized behavior of orbitals from a bulk material. We will rather speak of a localized state, i.e. such a state won't take part to the transport properties of a semiconductor material as it is usually the case for delocalized states. It will rather be a hindrance to the mobility of free carriers (electrons and holes). The corresponding electronic states will not contribute to the continuum of states of a bulk material. They will lie instead in the band gap of the semiconductor. The large surface density of states (i.e. dangling bonds) will provide to this two-dimensional system a continuum-like behavior on a given energy range.

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1 Poisson's equation applied to the vicinity of an n-type semiconductor surface such as the one displayed in Figure 1 will express as:

$$\frac{d^2V}{dz^2} = -\frac{eN_D}{\epsilon} \quad (\text{equation applied to the case of positive fixed charges of density equal to } N_D)$$

$$\text{i.e. } \frac{dV}{dz} = -E(z) = -\frac{eN_D}{\epsilon} z + K_1$$

Boundary conditions are such that in $z=0$ (origin of distances taken at the surface with the Oz axis oriented toward the semiconductor)

$K_1 = E_0$. As a result, we get $V(z) = -\frac{eN_D}{2\epsilon} z^2 + E_0 z + K_2$ (the electric field is pointing from positive charges to negative ones).

For $z=0$, $K_2 = V(0)$ so that $V(z) - V(0) = -\frac{eN_D}{2\epsilon} z^2 + E_0 z$

We wish to determine the critical length L beyond which the potential difference $V(L) - V(0)$ is fully screened, i.e. the length leading to $E(z) = 0$.

From the expression of $E(z)$ derived above, we get:

$$E_0 - \frac{eN_D}{\epsilon} L = 0 \quad \text{i.e.} \quad L = \frac{\epsilon E_0}{eN_D}$$

In addition, $V(L) - V(0) = -\frac{eN_D}{2\epsilon} L^2 + E_0 L$ and as $E_0 = \frac{eN_D L}{\epsilon}$,

we obtain:

$$\Delta V (= V(L) - V(0)) = -\frac{eN_D}{2\epsilon} L^2 + \frac{eN_D}{\epsilon} L^2 = \frac{eN_D}{2\epsilon} L^2$$

$$\text{so that } \boxed{L = \left(\frac{2\epsilon \Delta V}{eN_D} \right)^{1/2}}$$

It is seen that $\Delta V \propto \frac{\rho}{\epsilon} L^2$ where ρ is the fixed charge density

ΔV will also be called V_d (potential drop) in the next exercises

~~2~~ For a non-degenerate semiconductor in absence of any external perturbation, the average electron density in the conduction band is given by: $n_0 = N_c \exp(-(E_c - E_F)/k_B T)$ (Boltzmann approximation)

③ If now we add a slowly varying electrostatic potential $V(z)$ at the crystal lattice scale, each electron along z will possess, in addition to its energy arising from the crystal network, a potential energy $-eV(z)$. We can then understand that the whole conduction band will be shifted in energy by a quantity $-eV(z)$. As at thermal equilibrium the Fermi energy is constant throughout the material, the electron density will vary like:

$$n(z) = N_c \exp\left(-\frac{(E_c - eV(z) - E_F)}{k_B T}\right) \quad \text{i.e.} \quad n(z) = n_0 \exp\left(\frac{eV(z)}{k_B T}\right)$$

The charge induced by the potential is given by: $\rho_{\text{ind}}(z) = -e(n(z) - n_0)$
 i.e. $\rho_{\text{ind}}(z) = -en_0 \left[\exp\left(\frac{eV(z)}{k_B T}\right) - 1 \right] \approx -\frac{e^2 n_0}{k_B T} V(z) = -\epsilon q_D^2 V(z)$

→ valid in the limit of weak potentials!

The linearization of the built-in charge allows defining the Debye wave vector q_D and thus the Debye screening length $l_D = \frac{1}{q_D}$.

As a result, we get $l_D = \left(\frac{\epsilon k_B T}{e^2 n_0} \right)^{1/2}$ l_D corresponds to the length scale beyond which an electron gas can fully screen an external potential.

For silicon exhibiting a doping level of 10^{17} cm^{-3} at room temperature, we get ($\epsilon_r \sim 12$): $l_D = \left(\frac{12 \times 8.82 \times 10^{-12} \times 1.38 \times 10^{-23} \times 300}{(1.6 \times 10^{-19})^2 \times 10^{23}} \right)^{1/2} \sim 13.1 \text{ nm}$

I. Surface phenomena

② From Figure 1, we can immediately deduce that σ is given by

$$\sigma = -eN_{ss}(E_F - e\phi_0 - E_v(0))$$

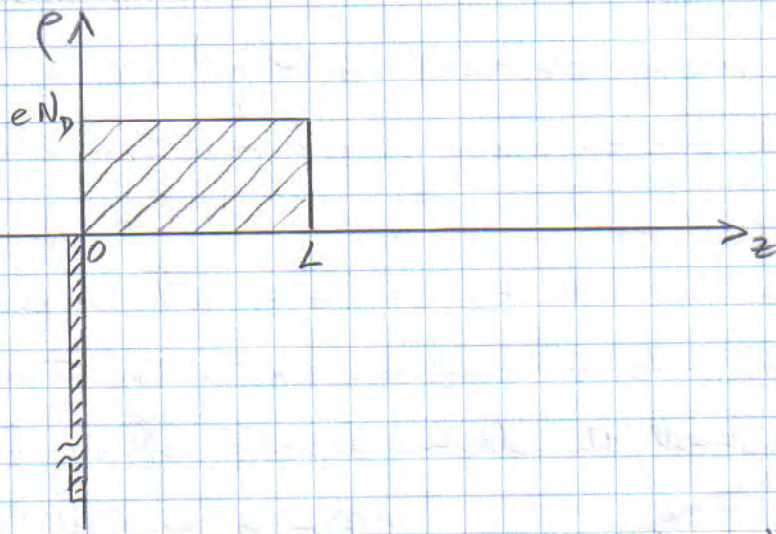
③ As we must satisfy electrical neutrality, the surface charge σ will correspond to the charge spread over the space charge region so that

$$-\sigma = eN_D L \quad \text{and thus} \quad V_D = -\frac{\sigma L}{2\epsilon}$$

→ as seen on the figure hereafter!

to find it, express the result of Ex.1 to find $V_D = \dots$

and identify the presence of σ



From previous questions, we can derive that

$$V_d = \frac{L}{2\epsilon} e N_{ss} (E_F - e\phi_0 - E_V(0))$$

Moreover, $E_V(0) = E_V(+\infty) + eV_d$ so that

$$V_d = \frac{L}{2\epsilon} e N_{ss} (E_F - e\phi_0 - E_V(+\infty) - eV_d)$$

$$\text{i.e. } V_d \left(1 + \frac{e^2 L}{2\epsilon} N_{ss}\right) = \frac{eL}{2\epsilon} N_{ss} (E_F - e\phi_0 - E_V(+\infty))$$

In the limit of a large surface density, V_d will not depend on N_{ss} so that

$$eV_d = E_F - e\phi_0 - E_V(+\infty)$$

$$\text{i.e. } E_C(+\infty) - E_g + eV_d = E_F - e\phi_0 \quad \text{and since } E_C(0) = E_C(+\infty) + eV_d$$

$$\text{we finally get } \boxed{E_C(0) - E_F = E_g - e\phi_0}$$

II - The ideal Schottky junction

By analogy with question 2, we can write $n(0) = N_C \exp\left(-\frac{(E_C(0) - E_F)}{k_B T}\right)$.
In addition, $E_C(0) - E_F = E_g - e\phi_0 = e\phi_B$ (cf. Figs. 1 and 2)

$$\text{So that } \boxed{n(0) = N_C \exp\left(-\frac{e\phi_B}{k_B T}\right)}$$

When considering Boltzmann velocity distribution we get

$$\langle v_z \rangle = \frac{\int_{-\infty}^0 v_z \exp(-m_c^* v_z^2 / 2k_B T) dv_z}{\int_{-\infty}^0 \exp(-m_c^* v_z^2 / 2k_B T) dv_z} = -\left(\frac{2k_B T}{\pi m_c^*}\right)^{1/2}$$

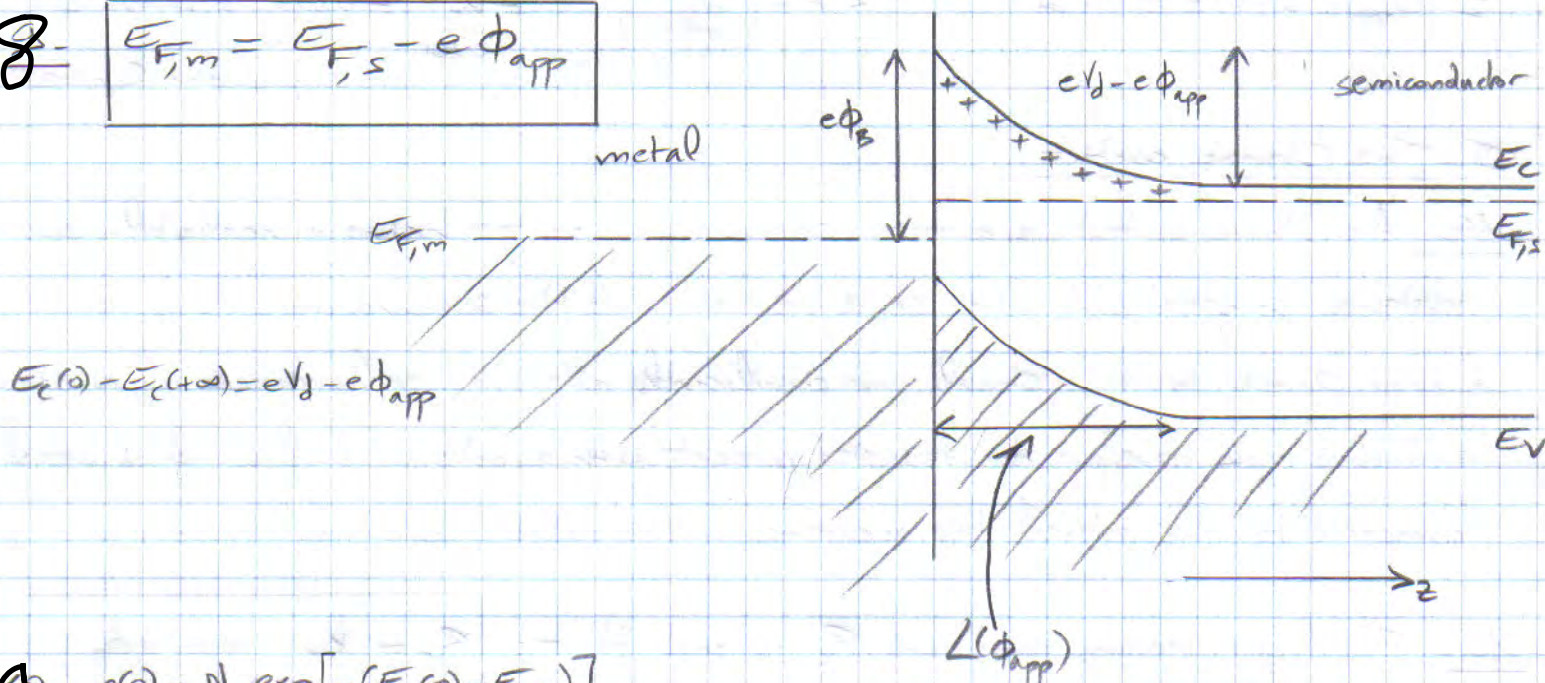
Average v_z of carriers travelling towards the left

(5)

7- The expression of $j_{s \rightarrow m}$ is given by $j_{s \rightarrow m} = -e n(0) \langle v_z \rangle$

so that
$$j_{s \rightarrow m} = e \left(\frac{k_B T}{2\pi m_e^*} \right)^{1/2} N_c \exp\left(-\frac{e\phi_B}{k_B T}\right)$$

8-
$$E_{F,m} = E_{F,s} - e\phi_{app}$$



9-
$$n(0) = N_c \exp\left[-\frac{(E_c(0) - E_{F,s})}{k_B T}\right]$$

i.e. $n(0) = N_c \exp\left[-\frac{(e\phi_B - e\phi_{app})}{k_B T}\right]$ and thus we get:

$$j_{s \rightarrow m} = e \left(\frac{k_B T}{2\pi m_e^*} \right)^{1/2} N_c \exp\left(-\frac{e\phi_B}{k_B T}\right) \exp\left(\frac{e\phi_{app}}{k_B T}\right)$$

because the two currents at equilibrium have opposite signs

10
$$j(\phi_{app}) = j_{s \rightarrow m} + j_{m \rightarrow s}$$

so that
$$j(\phi_{app}) = e \left(\frac{k_B T}{2\pi m_e^*} \right)^{1/2} N_c \exp\left(-\frac{e\phi_B}{k_B T}\right) \left[\exp\left(\frac{e\phi_{app}}{k_B T}\right) - 1 \right]$$

$j(\phi_{app})$ can thus be expressed as $j(\phi_{app}) = j_{sat} \left[\exp\left(\frac{e\phi_{app}}{k_B T}\right) - 1 \right]$ i.e. it exhibits a rectifying dependence and j_{sat} is given by:

$$j_{sat} = A^* T^2 \exp\left(-\frac{e\phi_B}{k_B T}\right)$$
 since $N_c = \frac{1}{4} \left(\frac{2m_e^* k_B T}{\pi \hbar^2} \right)^{3/2}$ with $A^* = \frac{4e k_B^2 \pi m_e^*}{h^3}$

11-
$$A^* = \frac{4 \times 1.6 \times 10^{-19} \times (1.38 \times 10^{-23})^2 \times \pi \times 9.1 \times 10^{-31}}{(6.62 \times 10^{-34})^3} \approx 120 \text{ A cm}^{-2} \text{ K}^{-2}$$

$$j_{\text{sat}} = A^* \frac{m_c^*}{m_0} T^2 \exp\left(-\frac{e\phi_B}{k_B T}\right) \text{ i.e. } j_{\text{sat}} = 120 \times 0.067 \times 300^2 \exp\left(-\frac{0.7}{0.025}\right) = 0.5 \mu\text{A}/\text{cm}^2 \quad (6)$$

$$I_{\text{sat}} = 0.05 \text{ nA}, \quad I(\phi_{\text{app}} = 0.2 \text{ V}) = I_S \left[\exp\left(\frac{0.02}{0.025}\right) - 1 \right] = 0.15 \mu\text{A}$$

$$I(\phi_{\text{app}} = 0.4 \text{ V}) = 0.44 \text{ mA}$$

$$R_0 A = \left(\frac{\partial j}{\partial \phi_{\text{app}}} \right)_{\phi_{\text{app}}=0}^{-1} = \frac{k_B T}{e j_{\text{sat}}} = \frac{0.025}{0.5 \times 10^{-6}} = 50 \text{ k}\Omega \text{ cm}^2 \text{ and } R_0 = 500 \text{ M}\Omega$$

III - The Ohmic contact

13 An Ohmic contact is a metal-semiconductor contact having a negligible contact resistance compared with the series resistance of the semiconductor. As a result, a good Ohmic contact should not significantly alter the performances of a device and thus can transfer the requested current with a potential drop which is small compared to the potential drop occurring in the active region of the device.

14 For light doping conditions R_c is such that: $R_c = \frac{k_B}{e A^* T} \exp\left(\frac{e\phi_B}{k_B T}\right)$

To obtain a low R_c value a metal-semiconductor contact exhibiting a small Schottky barrier height is to be preferred.

15 For heavy doping conditions the barrier thickness becomes relatively thin and is dominated by tunneling.

$$I \sim \exp\left[-2\kappa (2m_c^* (e\phi_B - e\phi_{\text{app}})/\hbar^2)^{1/2}\right] \text{ and } \kappa^2 \sim \frac{2E}{\hbar^2} (\phi_B - \phi_{\text{app}})$$

$$\text{so that } I \sim \exp\left[-\frac{4(m_c^* E)^{1/2} (\phi_B - \phi_{\text{app}})}{\hbar N_D^{1/2}}\right]$$

$$\text{and } R_c \sim \exp\left[\frac{4(m_c^* E)^{1/2} \phi_B}{\hbar N_D^{1/2}}\right] \propto \exp\left(\frac{\phi_B}{N_D^{1/2}}\right)$$

R_c exhibits a strong dependence on the doping level